

(15) **Today**

4.4 Uses of Character Tables

Next Class (16)

4.4 Uses of Character Tables

(17) **Second Class from Today**

5.1 Formation of Molecular Orbitals

5.2 Homonuclear Diatomic Molecules

Third Class from Today (18)

5.2 Homonuclear Diatomic Molecules

5.3 Heteronuclear Diatomic Molecules

IR active vibrations in H_2O

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz
Γ	9	-1	3	1		

reducible representations

summary of all the symmetry associated with the movement of the atoms in H_2O

find which irreducible representations to find symmetry for individual motions not as a group

number of irreducible representations of a given type needed = $\frac{1}{\text{order}} \sum_{\text{classes}} \left[\begin{matrix} \# \\ \text{operations} \\ \text{in class} \end{matrix} \right] \left[\begin{matrix} \chi \text{ of the} \\ \text{irreducible} \\ \text{representation} \end{matrix} \right] \left[\begin{matrix} \chi \text{ of the} \\ \text{reducible} \\ \text{representation} \end{matrix} \right]$

order = 1 + 1 + 1 + 1 = the number of operations in all classes

$$n(A_1) = \frac{1}{4} \cdot [(1)(1)(9) + (1)(1)(-1) + (1)(1)(3) + (1)(1)(1)]$$

$$n(A_1) = 3$$

C _{2v}	E	C ₂	σ _v (xz)	σ _v (yz)		
A ₁	1	1	1	1	z	x ² , y ² , z ²
A ₂	1	1	-1	-1	R _z	xy
B ₁	1	-1	1	-1	x, R _y	xz
B ₂	1	-1	-1	1	y, R _x	yz
Γ	9	-1	3	1		

order = 1² + 1² + 1² + 1² = sum of the squares of the χ under E

number of irreducible representations of a given type needed = $\frac{1}{\text{order}} \sum_{\text{classes}} \left[\begin{matrix} \star \\ \# \\ \text{operations} \\ \text{in class} \end{matrix} \right] \left[\begin{matrix} \star \\ \chi \text{ of the} \\ \text{irreducible} \\ \text{representation} \end{matrix} \right] \left[\begin{matrix} \star \\ \chi \text{ of the} \\ \text{reducible} \\ \text{representation} \end{matrix} \right]$

n must be a whole #

if it's not, double check your math

$$n(A_2) = \frac{1}{4} \cdot [(1)(1)(9) + (1)(1)(-1) + (1)(-1)(3) + (1)(-1)(1)]$$

9 - 5 = 4

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz
Γ	9	-1	3	1		

$n(A_2) = 1$

$$\begin{matrix} \text{number of} \\ \text{irreducible} \\ \text{representations} \\ \text{of a given type} \\ \text{needed} \end{matrix} = \frac{1}{\text{order}} \sum_{\text{classes}} \left[\begin{matrix} \# \\ \text{operations} \\ \text{in class} \end{matrix} \right] \begin{matrix} \chi \text{ of the} \\ \text{irreducible} \\ \text{representation} \end{matrix} \begin{matrix} \chi \text{ of the} \\ \text{reducible} \\ \text{representation} \end{matrix} \right]$$

$$n(B_1) = 1/4 \cdot [(1)(1)(1) + (1)(1)(1) + (1)(1)(1) + (1)(1)(1)]$$

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz
Γ	9	-1	3	1		

$$\begin{array}{l} \text{number of} \\ \text{irreducible} \\ \text{representations} \\ \text{of a given type} \\ \text{needed} \end{array} = \frac{1}{\text{order}} \sum_{\text{classes}} \left[\begin{array}{c} \# \\ \text{operations} \\ \text{in class} \end{array} \right] \left[\begin{array}{c} \chi \text{ of the} \\ \text{irreducible} \\ \text{representation} \end{array} \right] \left[\begin{array}{c} \chi \text{ of the} \\ \text{reducible} \\ \text{representation} \end{array} \right]$$

$$n(\text{B}_2) = 1/ \cdot [(\)(\)(\) + (\)(\)(\) + (\)(\)(\) + (\)(\)(\)]$$

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz
Γ	9	-1	3	1		

C _{2v}	E	C ₂	σ _v (xz)	σ _v (yz)		
A ₁	1	1	1	1	z, z	x ² , y ² , z ²
A ₂	1	1	-1	-1	R _z	xy
B ₁	1	-1	1	-1	x, R _y	xz
B ₂	1	-1	-1	1	y, R _x	yz
Γ	9	-1	3	1		

If we had an A₂ vibration it would be IR inactive

Γ = 3A₁ + A₂ + 3B₁ + 2B₂

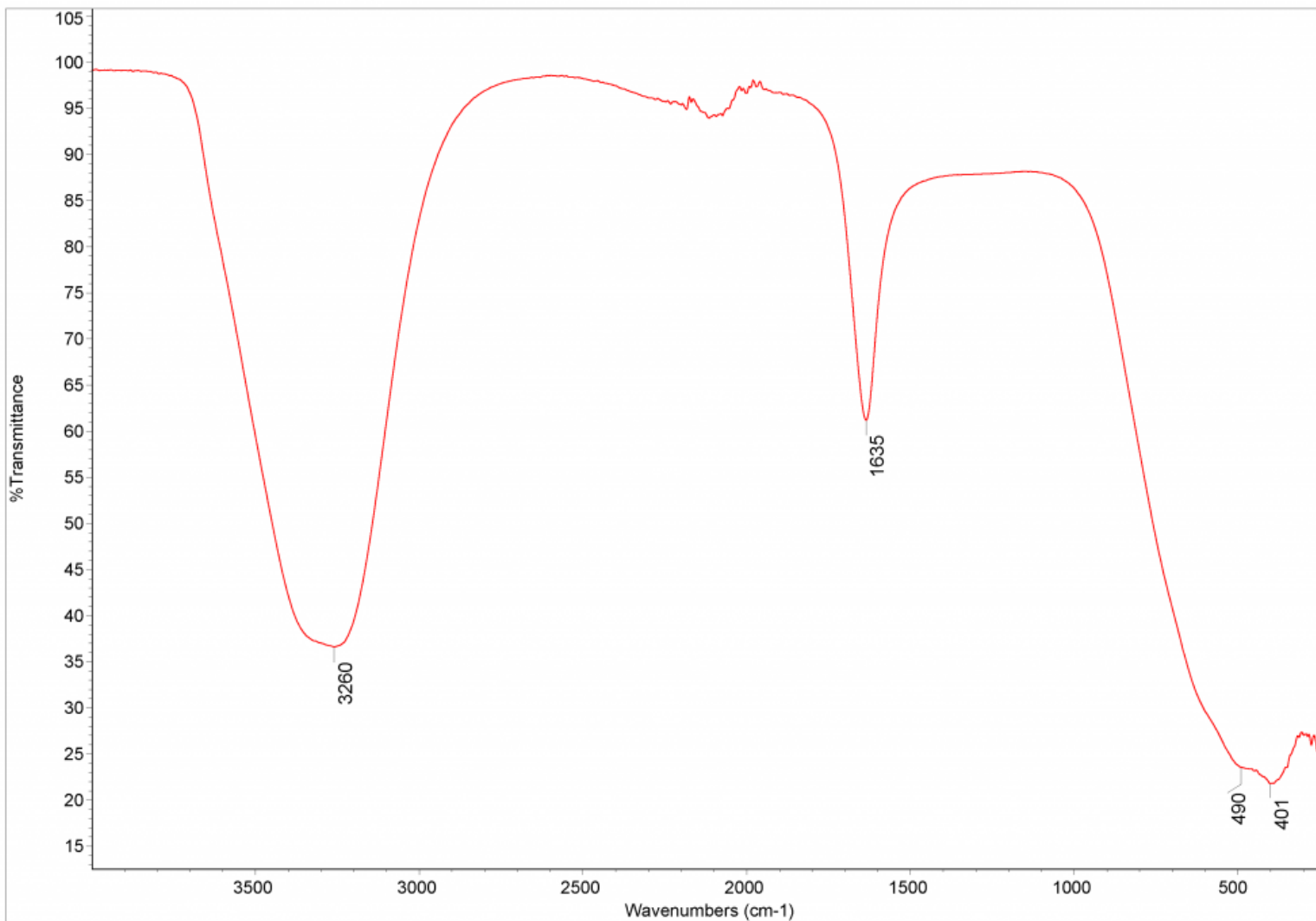
move along x, y, + z axes

all possible motions = vibration + translation + rotation

$$\text{number of vibrational modes} = \left(\begin{matrix} \text{\# of ways} \\ \text{of moving} \\ \cancel{A_1} \ A_1 \ A_1 \\ \cancel{A_2} \end{matrix} \right) - \left(\begin{matrix} \text{translational} \\ \text{movement} \\ \cancel{A_1} \ + \ \cancel{B_1} \ + \ \cancel{B_2} \end{matrix} \right) - \left(\begin{matrix} \text{rotational} \\ \text{movement} \\ \cancel{A_2} \ + \ \cancel{B_1} \ + \ \cancel{B_2} \end{matrix} \right)$$

3 IR active vibrations
3 peaks in IR spectrum

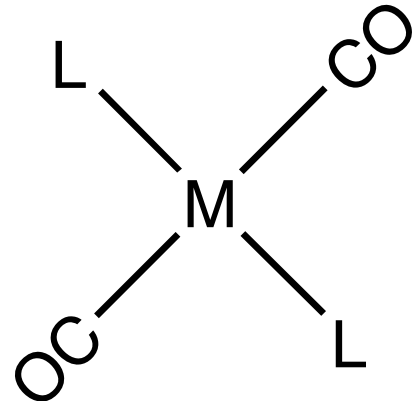
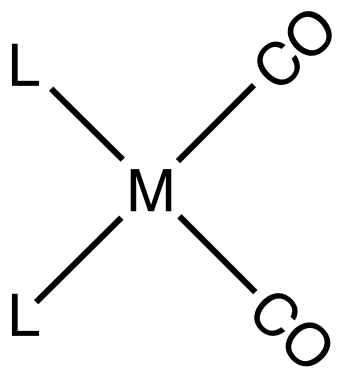
2 A₁ + B₁ symmetry of vibrational modes



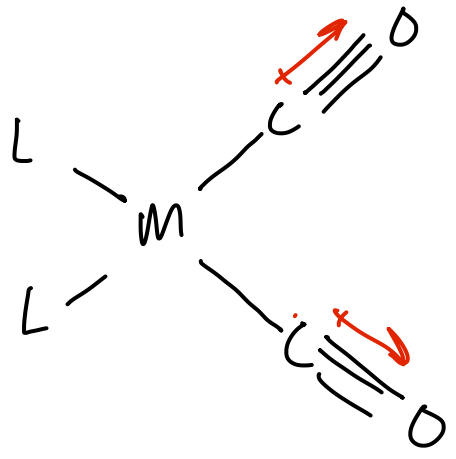
Carbonyl Stretching Bands in Metal Compounds: How Many?

$C\equiv O$ bonded to metal will stretch +
can change the dipole of the molecule

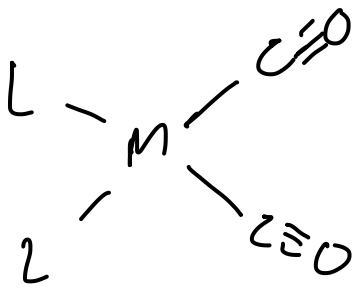
↑
intense 1715 cm^{-1}
Section 4.4
IR absorbance



↕

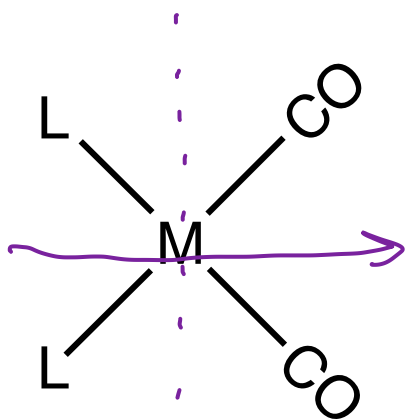


⇔



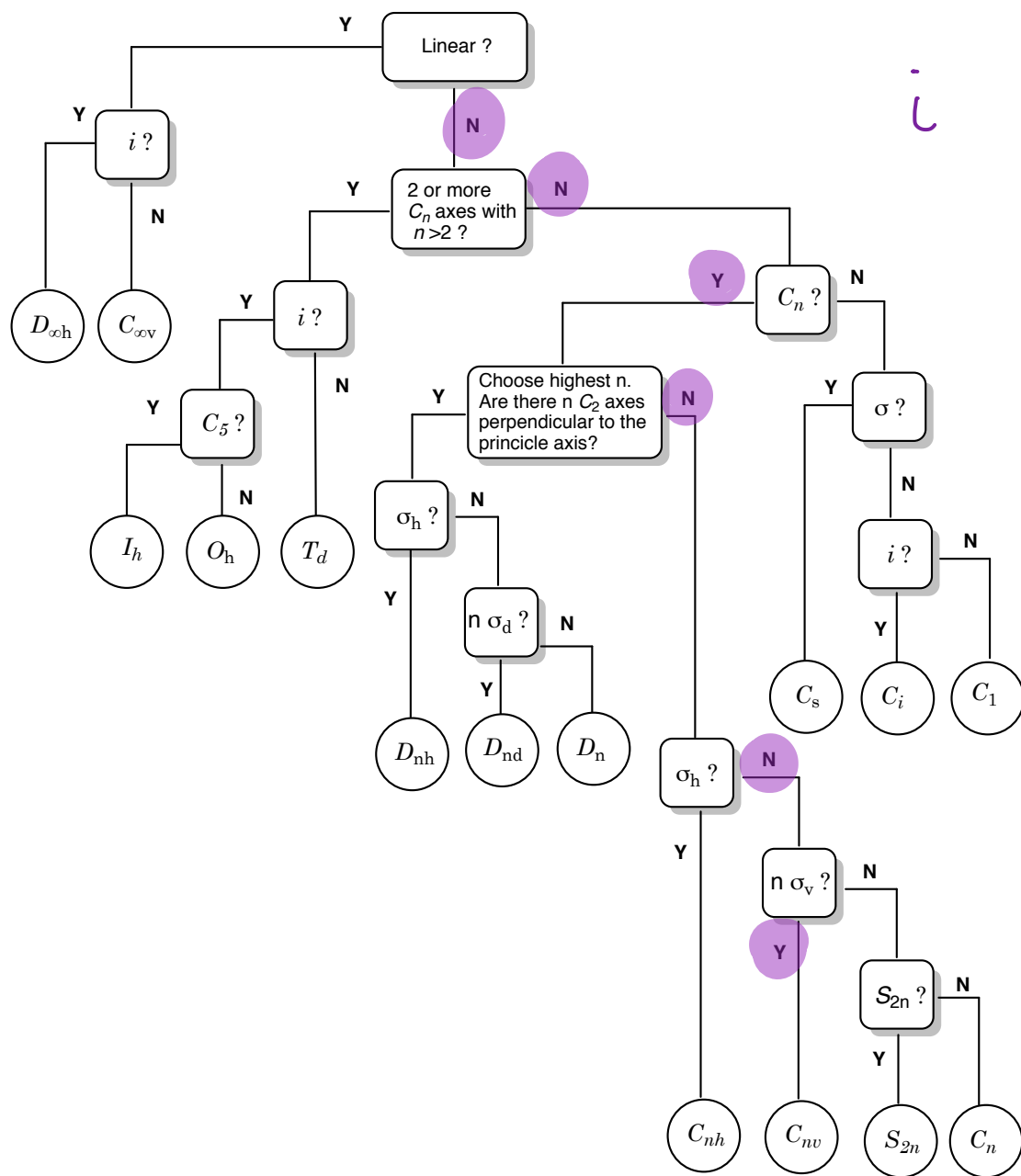
Carbonyl Stretching Bands in Metal Compounds: Find Point Group

Section 4.4



σ_h ?
cut in half
on line \perp to
 C_2 ? No

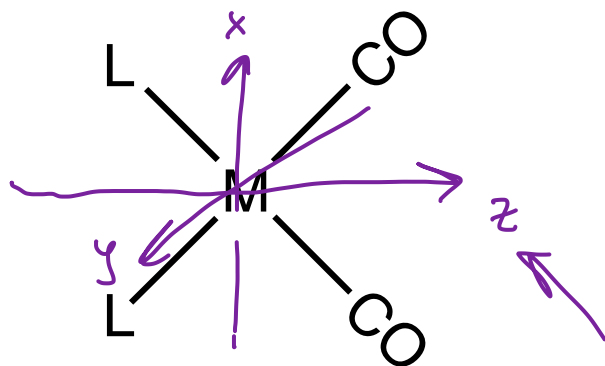
A σ_v contains the
principle axis.
are there 2? yes



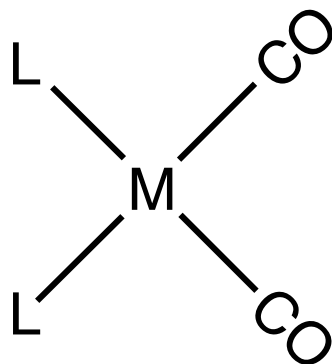
C_{2v}

C_{2h}

principle axis = z axis



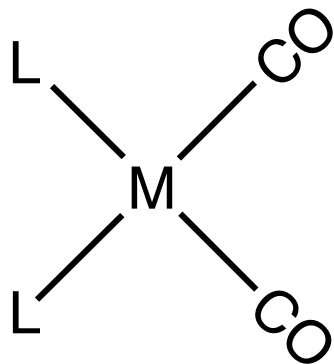
Carbonyl Stretching Bands in Metal Compounds: Determine Reducible Representation



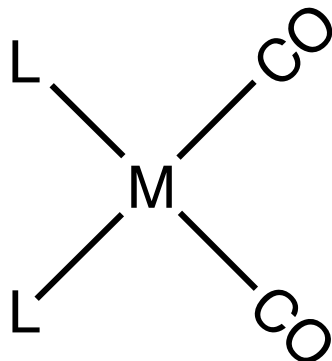
C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz

Γ

Carbonyl Stretching Bands in Metal Compounds: Determine Irreducible Representations that Combine to Form Reducible Representation



C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz
Γ	2	0	2	0		



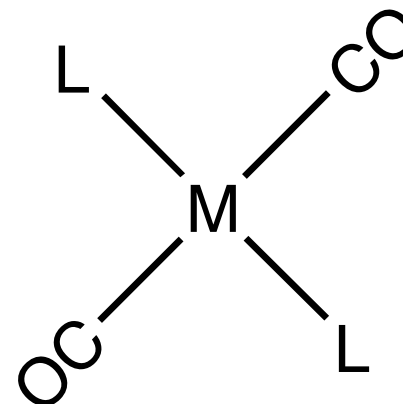
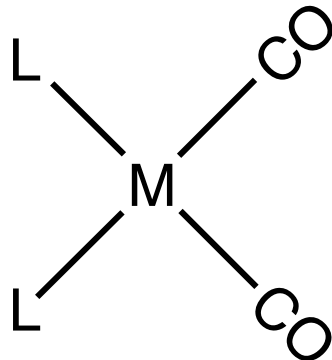
C _{2v}	E	C ₂	σ _v (xz)	σ _v (yz)		
A ₁	1	1	1	1	z	x ² , y ² , z ²
A ₂	1	1	-1	-1	R _z	xy
B ₁	1	-1	1	-1	x, R _y	xz
B ₂	1	-1	-1	1	y, R _x	yz

$$\Gamma \quad 2 \quad 0 \quad 2 \quad 0$$

$$\Gamma \quad = \quad A_1 \quad + \quad B_1$$

Carbonyl Stretching Bands in Metal Compounds (now the other one)

Section 4.4



Find Point Group

Assign Axes

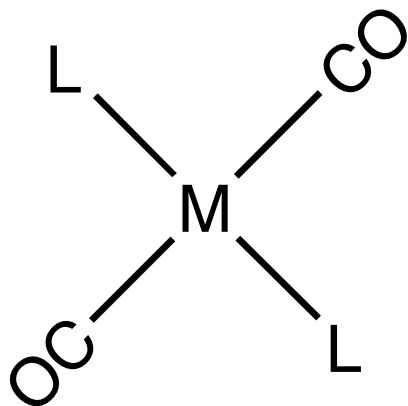
Determine Reducible Representation

Determine Irreducible Representations that Combine to Form Reducible Representation

Analyze Results

Carbonyl Stretching Bands in Metal Compounds (now the other one)

Section 4.4



D_{2h}	E	$C_2(z)$	$C_2(y)$	$C_2(x)$	i	$\sigma_h(xy)$	$\sigma_d(xz)$	$\sigma_d(yz)$		
A_g	1	1	1	1	1	1	1	1		x^2, y^2, z^2
B_{1g}	1	1	-1	-1	1	1	-1	-1	R_z	xy
B_{2g}	1	-1	1	-1	1	-1	1	-1	R_y	xz
B_{3g}	1	-1	-1	1	1	-1	-1	1	R_x	yz
A_u	1	1	1	1	-1	-1	-1	-1		
B_{1u}	1	1	-1	-1	-1	-1	1	1	z	
B_{2u}	1	-1	1	-1	-1	1	-1	1	y	
B_{3u}	1	-1	-1	1	-1	1	1	-1	x	
Γ	2	0	0	2	0	2	2	0		

