

(10) **Today**

4.1 Symmetry elements and Operations

4.2 Point Groups

**Next Class (11)**

4.1 Symmetry elements and Operations

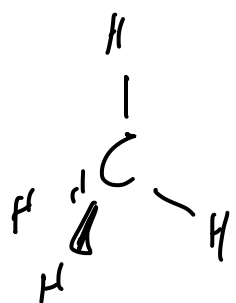
4.2 Point Groups

(12) **Second Class from Today**

4.3 IR Spectroscopy and Character Tables

**Third Class from Today**

Test 1 on Chap 1 through 4.2



There are a lot of symmetry operations for methane...

There is another way to find all the symmetry operations

In mathematics, a group is a **set** combined with an **operation** that has the specific mathematical properties

- the operation combines any two elements of the set to form a third element which is part of the original set

  - other ways of saying this:

  - a set must be closed under the operation

  - there must be closure with respect to the operation

- operating on elements of the set must satisfy the associative property

- there must be an identity element in the set that when operated on by the operation along with any element of the set returns the original element

- the operation in the set must be invertible; that is, the set must contain elements such that the operation on two elements in the set produce the identity element

## What is a Point Group?

## Section 4.3

It is a collection of symmetry operations with at least one fixed point that satisfies the criteria of being a mathematical "group"

$C_{2v}$

E	$C_2$	$\sigma_v(xz)$	$\sigma_v(yz)$
---	-------	----------------	----------------

The set is the set of symmetry operations.

The operation is the symmetry operations operating on each other.

$$C_2 \times \sigma_v(xz) = \sigma_v(yz) \quad C_2 \times \sigma_v(yz) = \sigma_v(xz) \quad \sigma_v(xz) \times \sigma_v(yz) = C_2$$

$$C_2 \times (\sigma_v(xz) \times C_2) = \sigma_v(xz) \quad (C_2 \times \sigma_v(xz)) \times C_2 = \sigma_v(xz)$$

$$E \times C_2 = C_2$$

$$C_2 \times C_2 = E$$

$C_s$   $C_i$

$C_1$   $C_2$   $C_3$   $C_4$   $C_5$   $C_6$   $C_7$   $C_8$

$C_{2v}$   $C_{3v}$   $C_{4v}$   $C_{5v}$   $C_{6v}$

$C_{2h}$   $C_{3h}$   $C_{4h}$   $C_{5h}$   $C_{6h}$

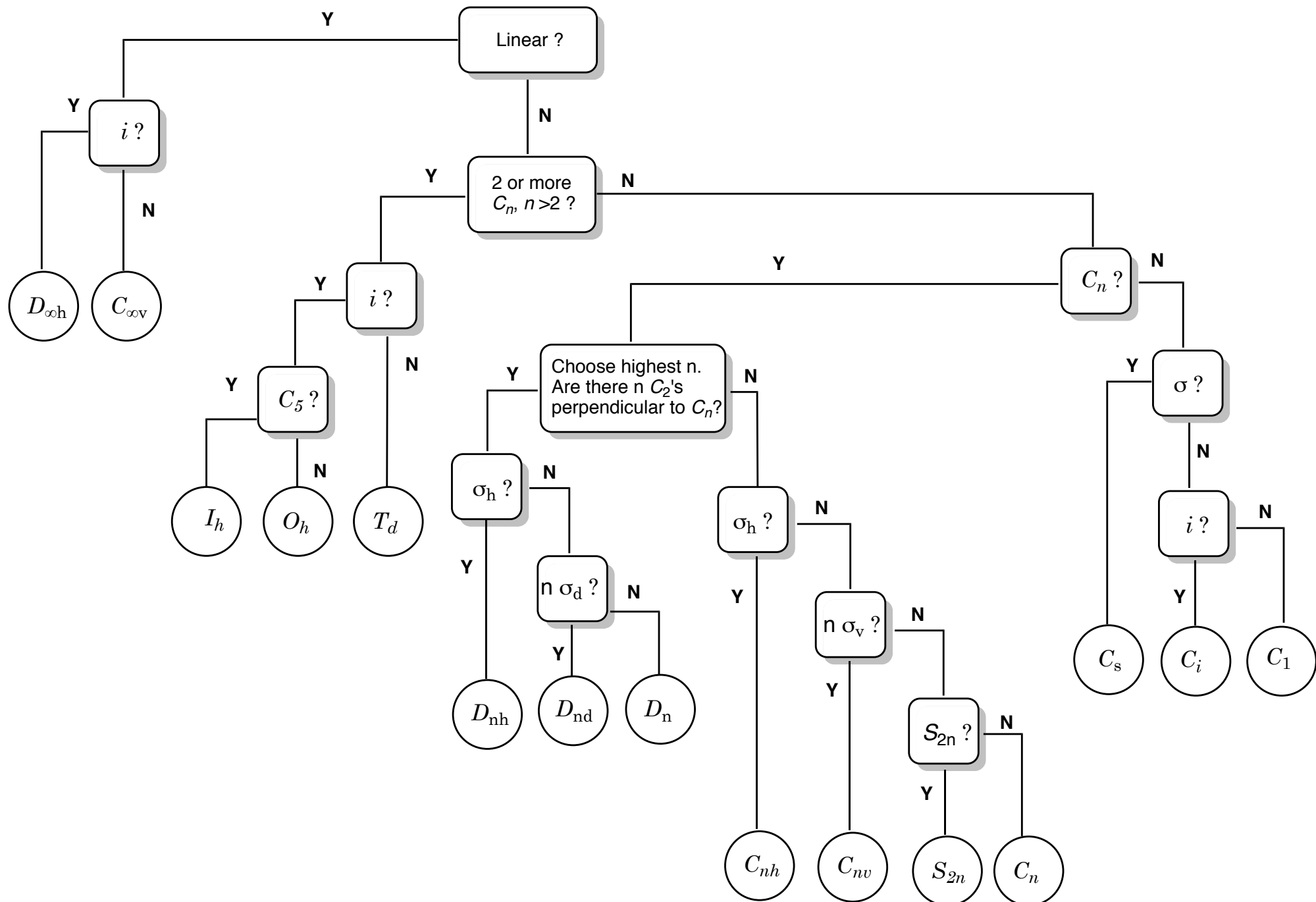
$D_1$   $D_2$   $D_3$   $D_4$   $D_5$   $D_6$

$D_{2d}$   $D_{3d}$   $D_{4d}$   $D_{5d}$   $D_{6d}$

$D_{2h}$   $D_{3h}$   $D_{4h}$   $D_{5h}$   $D_{6h}$   $D_{8h}$

$C_{\infty v}$   $D_{\infty h}$

$T$   $T_d$   $T_h$   $O$   $O_h$   $I$   $I_h$



# Using the Tree

## Section 4.2

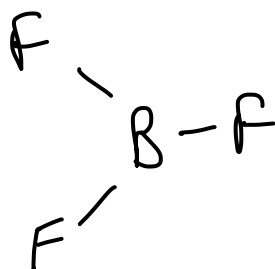
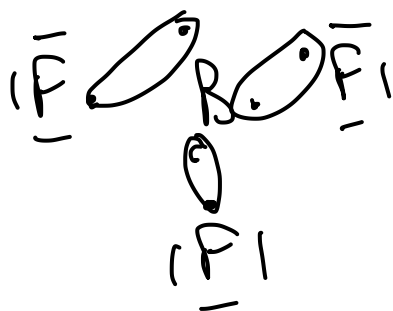
BF<sub>3</sub>

D<sub>3h</sub>

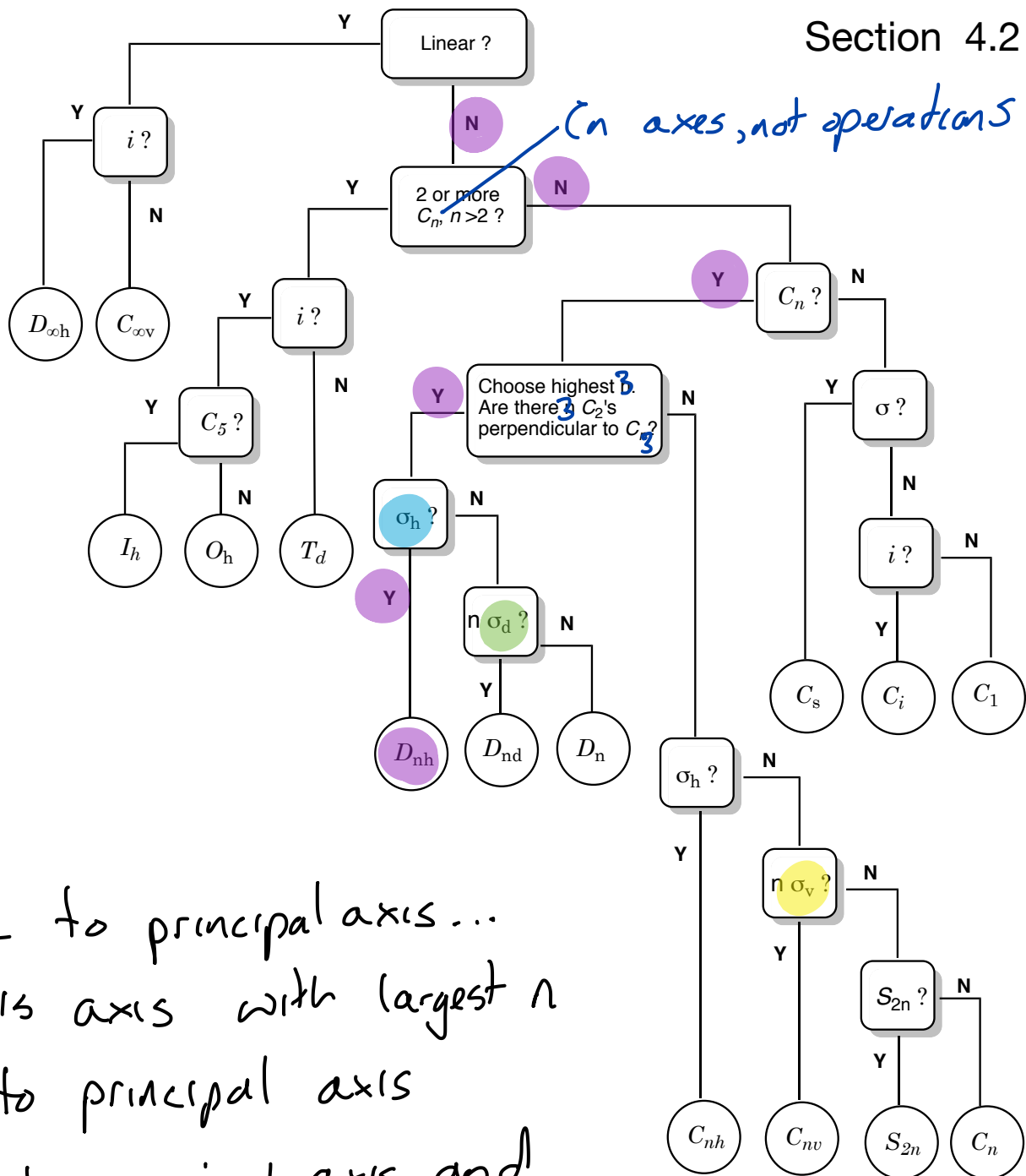
Lewis structure

VSEPR

Symmetry



- $\sigma_h$  mirror plane  $\perp$  to principal axis...  
principal axis is axis with largest  $n$
- $\sigma_v$  mirror plane  $\parallel$  to principal axis
- $\sigma_d$  mirror plane  $\parallel$  to principal axis and  
bisects 2  $C_2$  axes



# Practice

## Section 4.2

